

II. FORMALIZATION OF CUTTING EFFORT MODEL

The theoretical model presented in this work is based on the theory of predictive machining [9]. The tool is a cutter diameter D_0 , length L_0 and of NT teeth. It is discretized in elementary slices of constant thickness dz , perpendicular to its main axis, and powered by a cutting motion M_c whose N is the frequency of rotation around its axis (Fig. 1). The force exerted on a cutting edge is obtained by summation of the force components which are applied to each slice. A summation over all the edges engaged in the material allows to obtain the total force exerted on the tool at a given time.

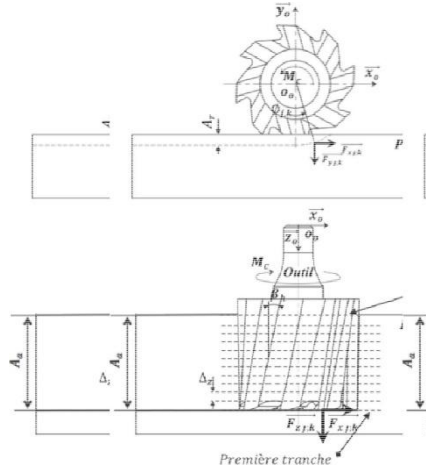


Figure 1 Modeling of cutting forces

The angular position of a tooth in contact with the workpiece is determined by the, , and radial , the number of teeth NT , the diameter of the tool D and, axial depth of cut, A_a at a certain place on the cutting edge can be, helix angle β . Instant this approximated as follows (Equ. 1)

$\theta_j = \beta + \frac{2\pi}{NT} (j-1) + \frac{2\pi}{NT} N t$, of the j , f , tooth at the, elementary

With, f , is the feed per tooth and, θ_j , is the angular position relative to the axis, disc k . Its, value changes

throughout the axial, direction as follows (Equ. 2):, $\theta_j = \beta + \frac{2\pi}{NT} (j-1) + \frac{2\pi}{NT} N t + \frac{2\pi}{NT} N z$, & !. & 1

, , , ,)*, ,)/0, 12 34, , (2), ,

Or N is the speed of rotation of the tool (tr/min), t is the time (min), D is the diameter of the cutter. Cutting actions can be modeled as oblique cut, using the theory of predictive machining [9]. Where cutting forces can be calculated from data on the properties of the material being machined, the tool geometry and cutting parameters. The basis of this theory is the analysis of the stress distribution along the shear plane and the tool-chip interface in terms of the angle of the shear plane ϕ and the properties of the machined material.

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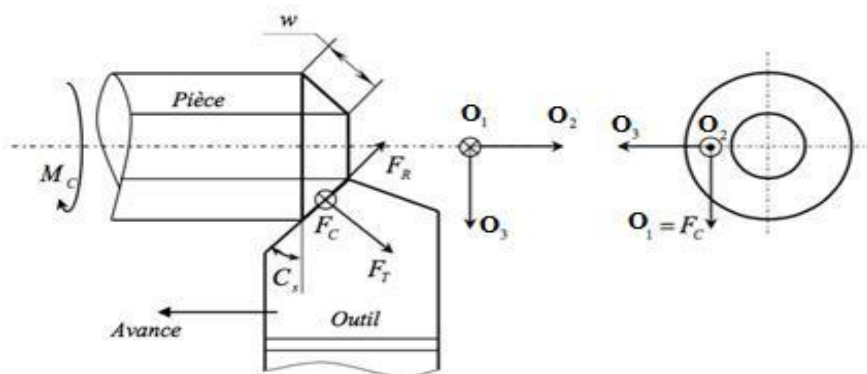


Figure 2 Modèle d'efforts de coupe pour la coupe oblique [1]

According to the theory[9], for an oblique cutting process, the actions of cutting forces in the cutting direction, feed and radial: (O_1) , (O_2) et (O_3) respectively as shown in the figure (Figure 2), are given by the equations (Equ. 3):, , ,

$O_1 = F_C \sin \phi$, $O_2 = F_C \cos \phi$, $O_3 = F_T$

$F_c = F \cos(\lambda)$ (3),

$F_r = F \sin(\lambda)$ & $F_a = F \cos(\psi)$

the, Taking F_c , F_r et F_a , will be the components of the cutting force in x , cutting direction, y , in advance and respectively, radial, and z can, therefore be determined using the equations (Equ. 4), (Equ. 5) et (Equ. 6)

$F_c = F \cos(\lambda)$ & $F_r = F \sin(\lambda)$ (4),

(5), $F_a = F \cos(\psi)$, $F_c = F \sin(\psi)$, $F_r = F \sin(\psi) \sin(\lambda)$, $F_a = F \cos(\psi) \sin(\lambda)$, $F_r = F \sin(\psi) \cos(\lambda)$, $F_a = F \cos(\psi) \cos(\lambda)$, (6),

With λ is the average angle of friction at the tool-chip interface, ψ is the cutting angle, ψ is the angle of inclination of the tool and, ϕ is the angle of the chip flow., These components of the force obliquely cut are calculated F_c , F_r , F_a ,

from the resulting R ,

strength in the shear plane and the tool-chip interface, it is given from the equation (Equ. 7)

$R = \frac{\tau_s h}{\sin(\phi)}$, (7), With τ_s is the shear stress in the primary shear zone, h is the thickness of undeformed section, ϕ is the angle between the resultant of the cutting forces R and the shear plane and w_c cutting width is it determined from the following equation (Equ., 8), $R = \frac{\tau_s h}{\sin(\phi)}$

(8), Since the action of each segment cutting is regarded as an oblique section with an angle of cut equal to the helix angle, the resultant force is given by the equation (Equ.

According to (Li XP, 1994, Zheng HQ, 1999), in milling, chip thickness varies with the time or position of the tool in the workpiece, and in the static mode the chip thickness is given by the following relationship (Equ. 10):, , ,

$h_c = \frac{D}{2} \sin^2(\alpha) \left(\frac{v_f}{v} - \frac{v_f}{v} \cos(\alpha) \right)$, (10),

$h_c = \frac{D}{2} \sin^2(\alpha) \left(\frac{v_f}{v} - \frac{v_f}{v} \cos(\alpha) \right)$, , ,

With α is the angle of entry into the material and, β is the exit angle, these,

angles are given⁸, for the cut milling by the equation (Equ. 11), and climb milling by,

$\alpha = \arccos\left(\frac{D - \sqrt{D^2 - 4Ar}}{2D}\right)$, , ,

the equation (Equ. 12), with D is the diameter of the milling cutter and Ar is the radial depth of cut:

$\alpha = \arccos\left(\frac{D - \sqrt{D^2 - 4Ar}}{2D}\right)$, (11),

$\beta = \arccos\left(\frac{D + \sqrt{D^2 - 4Ar}}{2D}\right)$, , ,

$\beta = \arccos\left(\frac{D + \sqrt{D^2 - 4Ar}}{2D}\right)$, t, (12),

$\beta = \arccos\left(\frac{D + \sqrt{D^2 - 4Ar}}{2D}\right)$, , ,

To predict the cutting forces using a helical cutter, and to express the geometry of the cutter based on the work of (H.Z. Li, W.B. Zhang, X.P. Li, 2000). The prediction of cutting forces is determined from equations (Equ. 13) to cut milling and equations

(Equ. 14) to climb milling: , , , , ,

$F_c = F \cos(\lambda) \sin(\psi)$, $F_r = F \sin(\lambda) \sin(\psi)$, $F_a = F \cos(\psi) \sin(\lambda)$, (13),

$F_c = F \cos(\lambda) \sin(\psi)$, $F_r = F \sin(\lambda) \sin(\psi)$, $F_a = F \cos(\psi) \sin(\lambda)$, , ,

$F_c = F \cos(\lambda) \sin(\psi)$, $F_r = F \sin(\lambda) \sin(\psi)$, $F_a = F \cos(\psi) \sin(\lambda)$, , ,

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$F_c = F \cos(\lambda) \sin(\psi)$, $F_r = F \sin(\lambda) \sin(\psi)$, $F_a = F \cos(\psi) \sin(\lambda)$, , ,

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III. SIMULATION RESULTS FOR PERIPHERAL MILLING

In this section we present the simulation results for the case of the milling device for milling into opposition if the cutter is in the middle of the room

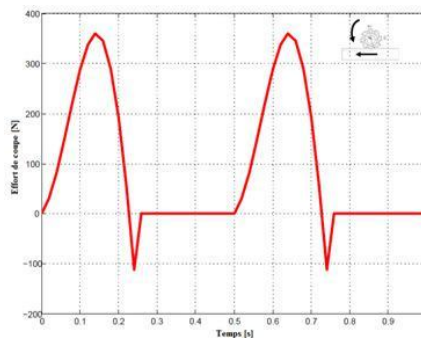


Figure 3 Fx Cutting effort to cut milling
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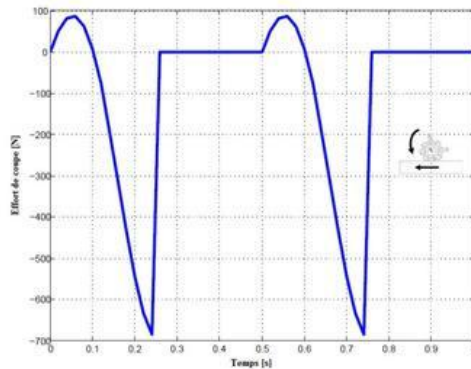


Figure 3 Fy Cutting effort to cut milling

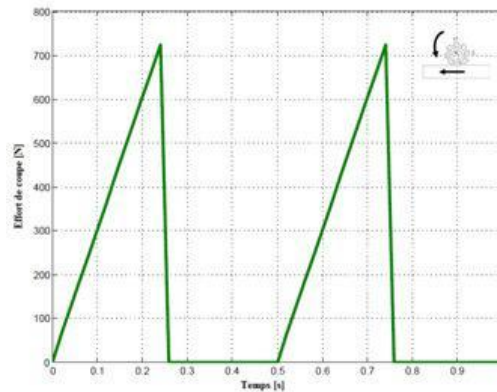


Figure 4 Fz Cutting effort to cut milling. Cutting forces F_x , F_y et F_z are simulated for the device with milling:

Table 1 simulation data

N [trs/s]	D[mm]	NT [dent]	f_t [mm/dent]	A_a [mm]	A_r [mm]	α	γ
2	10	1	0,1	8	10	0 °	460 x 10 ⁶

The figures 3, 4 et 5 show that for the case of cut milling, cutting efforts begin with zero values then they evolve in a progressive way, this increase explains the increase in the cutting section, the cutting force depends, then they cancel a brusque manner especially for efforts F_y et F_z , and it periodically, which explains the entrance of the tooth of the cutter into the material with a zero thickness

IV. PERIPHERAL MILLING LAYING DYNAMIC

This model was developed in view of processing the results of the simulation of the dynamic response of the peripheral section which causes the part of the movement. The difficulty of the task was to effectively bring needed. Indeed, the importance of geometric modeling is attached to the choice of model, which allows us, among other calculate all geometric parameters required for the temporal integration.

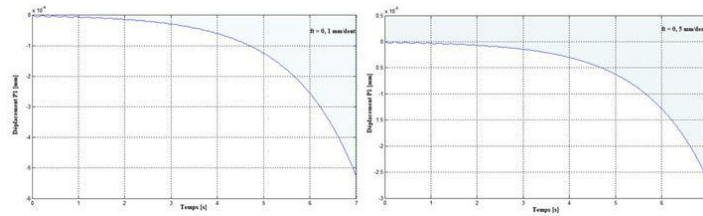


Figure 9 Move Support P1

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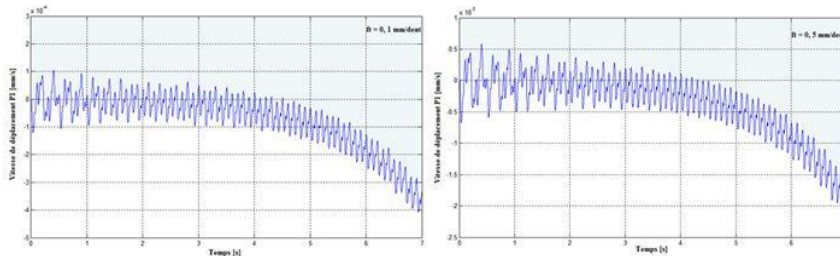


Figure 10 Travel speed Support P1

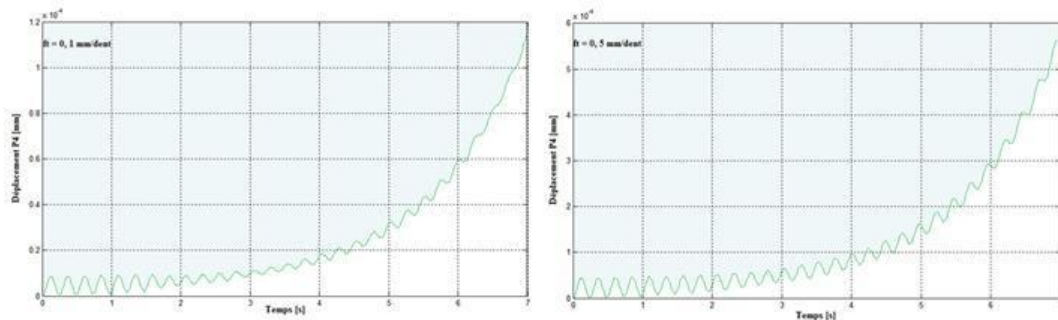


Figure 11 Move Support P4

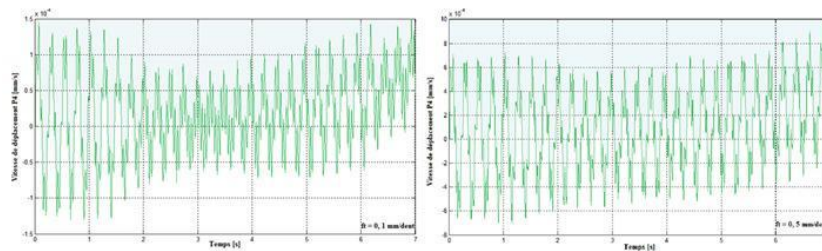


Figure 12 Travel speed Support P4

V. CONCLUSION

As conclusion, we can say that the axial depth is a value that affects the values of displacements of the cutter and cutting forces, and also we can say that this value affects the stability of the machining system. This simulation shows the dynamic response for two values of the feed per tooth (ft). For the case of cut milling, we notice that increasing the feed per tooth leads to increasing values of the displacements of the part and its speed. We clearly notice that the graphs of displacement and cutting forces retain the same forms of shapes but with increased amplitude. In conclusion, we can say that the feed per tooth influences the values of displacements of the part and on the cutting forces, and also can be said to affect the stability of the machining system.

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