

# An Application of Iterative Learning Control in Object Trajectory Tracking

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## Abstract

This paper presents an approach to trajectory tracking control using Iterative Learning Control (ILC) without requiring a mathematical model of the controlled system. Traditional control methods depend heavily on system modeling, which may not always be feasible due to system complexity or uncertainty. ILC offers a model-free alternative by utilizing repetition in tasks to iteratively improve control performance. The simulation results demonstrate that trajectory tracking accuracy improves as the number of learning iterations increases.

**Keywords:** Iterative Learning Control (ILC), Trajectory Tracking, Model-Free Control

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## I. Introduction

The ultimate goal of any automatic control system is to ensure that the system's output follows a desired reference trajectory. Most modern control strategies rely on an accurate mathematical model of the plant. However, due to external disturbances, non-linearities, or incomplete knowledge, obtaining such a model is not always practical. Iterative Learning Control (ILC) provides a solution by learning from previous executions of a repetitive task, progressively refining the control input to reduce tracking error over iterations.

## II. Problem Formulation

### 2.1. System Description

Consider a discrete-time single-input single-output (SISO) system represented by the transfer function:

$$W(z) = \frac{(z + 0.5)}{z^2 + 0.7z + 0.1} \quad (2.1)$$

The equation is represented a discrete - time transfer function

$$W(z^{-1}) = \frac{z^{-1} + 0.5z^{-2}}{1 + 0.7z^{-1} + 0.1z^{-2}} \quad (2.2)$$

This can be rewritten as the following difference equation:

$$y_k(t) = u_k(t-1) + 0.5u_k(t-2) - 0.7y_k(t-1) - 0.1y_k(t-2) \quad (2.3)$$

Where  $y_k(t)$  and  $u_k(t)$  are the output signal and input of the system at time  $t$

### 2.2. Learning Rule

The ILC algorithm updates the control input in the next iteration based on the error in the current iteration:

$$u_{k+1}(\tau) = u_k(\tau) + K \cdot e_k(\tau+1) \text{ for } 0 \leq \tau \leq T \quad (2.4)$$

## III. Simulation and Discussion

### 3.1. Simulation Setup

Learning gain:  $K = 0.5$

Initial conditions:  $y(1) = 1, y(2) = -1$

Simulation horizon:  $T = 60$

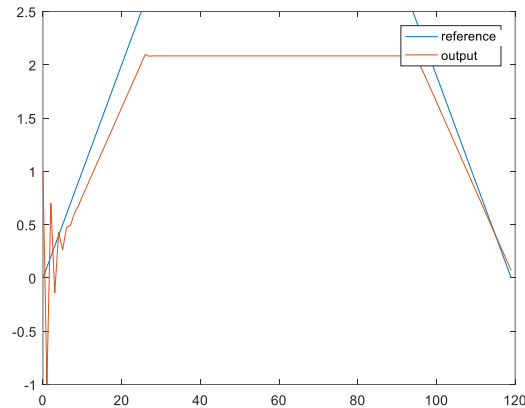
Reference signal:

$$r(t) = \begin{cases} 0.1t & (0 \leq t \leq 25) \\ 2.5 & (25 \leq t \leq 95) \\ -0.1(t - 95) + 2.5 & (95 \leq t \leq 120) \end{cases} \quad (2.5)$$

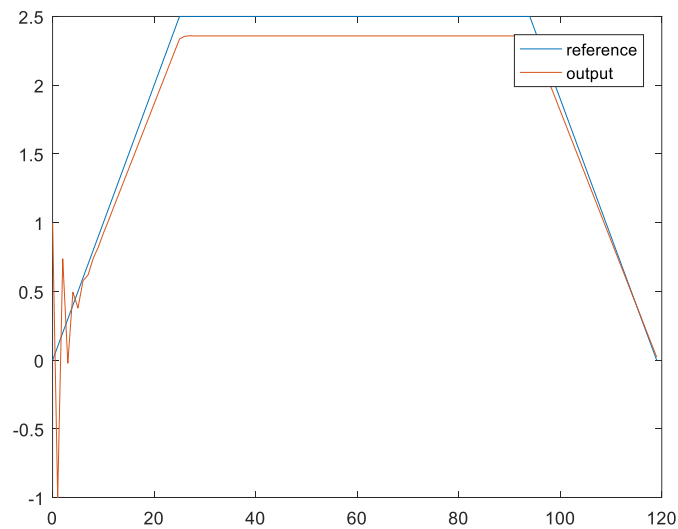
The control and learning algorithm is implemented in MATLAB to simulate multiple learning iterations.

### 3.2. Results

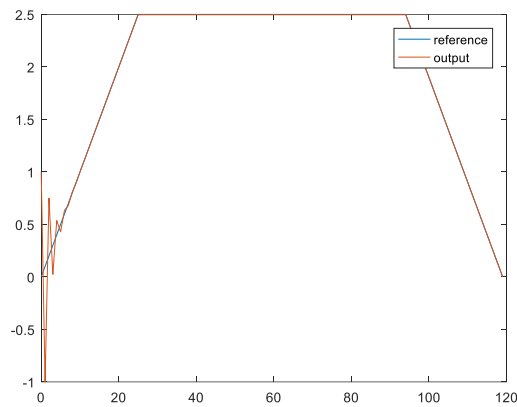
Iteration 1: The output signal begins to approximate the reference trajectory, but significant tracking errors remain.



Iteration 3: The control system shows improved tracking accuracy with reduced error.



Iteration 10: The system output closely follows the reference, indicating successful learning.



These results affirm the effectiveness of the ILC strategy in improving tracking performance over successive iterations.

#### **IV. Conclusion**

The study confirms that Iterative Learning Control can significantly enhance trajectory tracking performance in systems with repetitive operations, even in the absence of a precise mathematical model. The choice of learning law and tuning parameters plays a crucial role in convergence and effectiveness. Future work may explore robustness and generalization to nonlinear or time-varying systems.

#### **References**

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