

## Bulk transfer scheduling and path reservations in research networks

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**Abstract:** Data-intensive e-science collaborations often require the transfer of large files with predictable performance. To meet this need, we design novel admission control and scheduling algorithms for bulk data transfer in research networks for e-science. Due to their small sizes, the research networks can afford a centralized resource management platform. In our design, each bulk transfer job request, which can be made in advance to the central network controller, specifies a start time and an end time? If admitted, the network guarantees to complete the transfer before the end time. However, there is flexibility in how the actual transfer is carried out, that is, in the bandwidth assignment on each allowed paths of the job on each time interval, and it is up to the scheduling algorithm to decide this. To improve the network resource utilization or lower the job rejection ratio, the network controller solves optimization problems in making admission control and scheduling decisions. Our design combines the following elements into a cohesive optimization-based framework: advance reservation, multi-path routing, and bandwidth reassignment via periodic re-optimization. We evaluate our algorithm in terms of both network efficiency and the performance level of individual transfer. We also evaluate the feasibility of our scheme by studying the algorithm execution time.

**Keywords:** Admission control, Advance reservation, Bulk Data Transfer, E-Science, Grid Computing, Scheduling.

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### I. INTRODUCTION

The advance of communication and networking technologies together with the computing and storage technologies is dramatically changing the way show scientific research is conducted. A new term, *e-science*, has emerged to describe the “large-scale science carried out through distributed global collaborations enabled by networks, requiring access to very large scale data collections, computing resources, and high-performance visualization”[1]. Well-quoted e-science (and the related grid computing [2]) examples include high-energy nuclear physics (HEP), radio astronomy, geo science and climate studies.

The need for transporting large volume of data in e-science has been well-argued [3],[4].For instance, the HEP data is expected to grow from the current peta bytes (PB)( $10^{15}$ ) to exa bytes( $10^{18}$ ) by 2012 to 2015.In particular, the Large Hadron Collider facility at CERN is expected to generate peta bytes of experimental data every year, To meet the need of e-science, this paper studies *admission control* (AC) and *scheduling* algorithms for high-Band width data transfers (also known as jobs) in research networks .The results will not only advance the knowledge and techniques in that area, but also compliment the protocol, architecture and infrastructure projects currently under way in support of e-science and grid computing [9], [10], [11], by providing more efficient network resource reservation and management algorithms .Our AC and scheduling algorithms handle two classes of jobs, *bulk data transfer* and those that require a *minimum band width guarantee* (MBG).Bulk transfer is not sensitive to the network delay but may be sensitive to the delivery deadline. It is useful for distributing high volumes of scientific data, which currently often relies on ground transportation of the storage media .The MBG class is useful for real time rendering or visualization of data remotely. In our frame work, the algorithms for handling bulk transfer also contain

The need for efficient network resource utilization is especially relevant in the context of advance reservation and large file sizes or long-lasting flows. As argued in [13], there is an undesirable phenomenon known as *band width fragmentation*. The simplest example of bandwidth fragmentation occurs when the interval between the end time of one job and the beginning of another job is not long enough for any other job request. Then, the network or relevant links will be idle on that interval. If there are too many of these un-usable intervals or if their durations are long, the job rejection ratio is likely to be high while the network utilization remain slow. Over-provisioning the network capacity may not be the right solution due to the high cost, time delay or other practical constraints.

The solution advocated in this paper for reducing the job rejection ratio and increasing the network utilization Efficiency is to bring in more flexibilities in how the data are transferred. The process of determining the manner of data transfer is known as *scheduling*. For instance, one can take advantage of the elastic nature of

bulk data and have the network transferring the data at time-varying band width instead of a constant band width. Another example is to use multiple paths for each job. In order to achieve the greatest flexibilities, this paper formulate Recently, some authors have begun to study AC and scheduling for bulk transfer with advance reservations [14],[15],[16],[17],[18],[19],[13],[20],[21]. Compared with these earlier studies, our work distinguishes itself for its comprehensiveness in bringing several important ingredients together under a single optimization framework with well-defined objectives .These include (1) periodic admission control for handling continuous arrivals of job requests rather than ones hot admission control, (2) admission control and scheduling for the whole network rather than for each link separately ,(3) multi-path routing, (4) time-varying band width assignment for each job, (5) dynamic band width re-assignment at each AC/scheduling instance, which leaves more room to accept new requests, and (6) a novel timed iscretization scheme (i.e., the congruent time-slice structures) that allows the admission of new requests and band width re-allocation to existing jobs while not violating the end-time requirements of the existing jobs. As will be reviewed in Section 5, other studies in this area only in corporate a subset of the features from the above list.

The rest of the paper is organized as follows. The main technical contribution of this paper is to describe a suite of algorithms for AC and scheduling (Section 2) and compare their performance (Section 4). A key methodology is the discretization of time into a time slice structure so that the problems can be put into the linear programming framework. A highlight of our scheme is the introduction of non-uniform time slices (Section 3) ,which can dramatically shorten the execution time of the AC and scheduling algorithms ,making them practical. The related work is shown in Section 5 and the conclusion is drawn in Section 6.

## II. ADMISSIONCONTROLANDSCHEDULINGALGORITHMS

### 2.1) The Setup

For easy reference, notations and definitions frequently used in this paper are summarized in Appendix I. The network is represented as a (directed) graph  $G=(V,E)$ , where  $V$  is the set of nodes and  $E$  is the set of edges. The capacity of a link (edge)  $e \in E$  is denoted by  $C_e$ . Job requests arrive at the network following a random process. Each bulk transfer request  $i$  is a 6-tuple  $(A_i, s_i, d_i, D_i, S_i, E_i)$ , where  $A_i$  is the arrival time of the request,  $s_i$  and  $d_i$  are the source and destination nodes, respectively  $D_i$  is the size of the file,  $S_i$  and  $E_i$  are the requested start time and end time, where  $A_i \leq S_i \leq E_i$ . In words, request  $i$ , which is made at time  $t=A_i$ , asks the network to transfer a file of size  $D_i$  from nodes  $I$  to node  $d_i$  on the time interval  $[S_i, E_i]$ . A bulk transfer request may optionally specify a minimum bandwidth and/or a maximum bandwidth. In practice, even more parameters can be added if needed, such as an estimated range for the demand size or for the end times when the precise information is unknown [22]. For ease of presentation, we will ignore these options. But, they usually can be incorporated into our optimization-based AC/scheduling framework by modifying the formulations of the optimization problems. The approach of using a centralized network controller has an advantage here for an evolving system, since to accommodate new types of parameters or functions, the only necessary changes are at the central controller's software. The user-side software will be updated only if the user needs the new parameters or functions.

#### 2.1.1) The Time Slice Structure:

At each scheduling instance  $t=k\tau$ , the time line from  $t$  onward is partitioned into time slices i.e., closed intervals on the time line, which are not necessarily uniform in size. The significance of the time slice is that the bandwidth (rate) assignment to each job is done at the slice level. That is, the bandwidth assigned to a particular path of a job remains constant for the entire time slice, but it may change from slice to slice. A set of time slices,  $G_k$ , is said to be *anchored at*  $t=k\tau$  if all slices in  $G_k$  are mutually disjoint and their union forms an interval  $[t, t']$  for some  $t'$ . The set  $\{ G_k \}^\infty$  is called a *slice structure* if each  $G_k$  is a set of slices anchored at  $t=k\tau$ , for  $k=1, \dots, \infty$ .

*Definition1:* A slice structure  $\{ G_k \}_{k=1}^\infty$  is said to be **congruent** if the following property is satisfied for every pair of positive integers,  $k$  and  $k'$ , where  $k' > k \geq 1$ . For any slices  $s' \in G_{k'}$ , if  $s'$  overlaps in time with a slices,  $s, s \in G_k$ , then  $s' \subset s$ . In words, any slice in a later anchored slice collection must be completely contained in a slice of any earlier collection, if it overlaps in time with the earlier collection. Alternatively speaking, if slice  $s \in G_k$  overlaps in time with  $G_{k'}$ , the neither  $s \in G_{k'}$  or  $s$  is partitioned into multiple slices all belonging to  $G_{k'}$ . sized time slices of duration  $\tau$  (coinciding with the AC/scheduling interval length). The set of slices anchored at any  $t=k\tau$  is all the slices after  $t$ . Figure1 shows the US at two time instances  $t=\tau$  and  $t=2\tau$ . In this example,  $\tau=4$  time units. The arrows point to the scheduling instances. The two collections of rectangles are the

time slices anchored at  $t=\tau$  and  $t=2\tau$ , respectively. It is easy to check the congruent property of this slice structure.

The AC and scheduling algorithms introduced in this paper apply to any congruent slice structure. When a non-uniform slice structure is used, the congruent property is the key to the existence of algorithms that allow the network to keep the commitment to the old jobs admitted earlier while admitting new jobs. There is one key point on that, in solving the admission control problem, the bandwidth allocation (on each allowed path of each job) on each time slice is assumed to be constant. When a time slice is divided into finer slices at a later time, the old jobs are still admissible since one can keep the bandwidth on the finer slices at the same constant.<sup>2</sup> This will be further explained in Section 3. For ease of presentation, we use the uniform slices as an example to explain the AC and scheduling algorithms. At any AC/scheduling time  $t=k\tau$ , let the time slices anchored at  $t$ , i.e., those in  $G_k$ , be indexed 1,2,...in increasing order of time. Let the start and end times of slice  $i$  be denoted by  $ST_k(i)$  and  $ET_k(i)$ , respectively, and let its length be  $LEN_k(i)$ . We say a time instance  $t > t$  falls into slice  $i$  if  $ST_k(i) < t \leq ET_k(i)$ . The index of the slice that  $t$  falls inside noted by  $I_k(t)$ . At  $t=k\tau$ , let the set of jobs in the system yet to be completed be denoted by  $J_k$ .  $J_k$  contains two types of jobs, those new requests (also known as new jobs) made on the interval  $((k-1)\tau, k\tau]$ , denoted by  $J^N$ , and those old jobs admitted at or before  $(k-1)\tau$ , denoted by  $J^O$ . The old jobs have already been admitted and should not<sup>2</sup> However, one can often do better by varying the bandwidth on the finer slices.

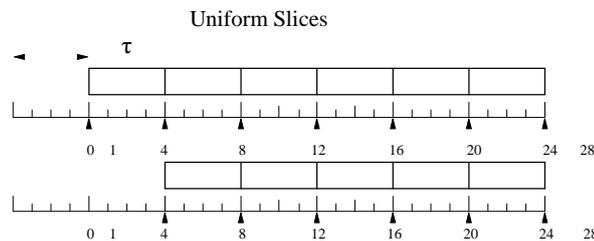


Fig.1. Uniform time slice structure be rejected by the admission control conducted at  $t$ . But some of the new requests may be rejected.

**2.1.2) Rounding of the Start and End Times:**

With the time slice structure and the advancement of time, we adjust the start and end times of the requests. The main objective is to align the start and end times on the slice boundaries. After such rounding, the start and the end times will be denoted as  $\hat{S}_i$  and  $\hat{E}_i$ , respectively. For a new request  $i$ , let the request end response time be  $T_i = E_i - S_i$ . We round the requested start time to be the maximum of the current time or the end time of the slice in which the requested start time  $S_i$  falls, i.e.,

$\hat{S}_i = \max \{ t, ET_k(I_k(S_i)) \}$ . (1) For rounding of the requested end time, we allow two policy choices, the *stringent policy* and the *relaxed policy*. Which one is used in practice is a policy issue, left to the decision of the network manager. In the stringent policy, if the requested end time does not coincide with a slice boundary, it is rounded down, subject to the constraint that  $\hat{E}_i > \hat{S}_i$ <sup>3</sup>. This constraint ensures that there is atleast one-slice separation between the rounded start time and the rounded end time. Otherwise, there is no way to schedule the job. In the relaxed policy, the end time is first shifted by  $T_i$  with respect to the rounded start time, and then rounded up. More specifically,

**stringent**

$$\hat{E}_i = \begin{cases} ET_k(I_k(\hat{S}_i) + 1) & \text{if } ST_k(I_k(E_i)) \leq \hat{S}_i \\ E_i & \text{else if } ET_k(I_k(E_i)) = E_i \\ ST_k(I_k(E_i)) & \text{otherwise.} \end{cases} \quad (2)$$

**relaxed**

$$\hat{E}_i = ET_k(I_k(\hat{S}_i + T_i))$$

Figure 2 shows the effect of the two policies after three jobs are rounded.<sup>3</sup> In the more sophisticated non-uniform slice structure introduced in Section 3, we allow the end time to be re-rounded at different scheduling instances. This way, the rounded end time can be closer to the requested end time, as the slice sizes become finer over time.

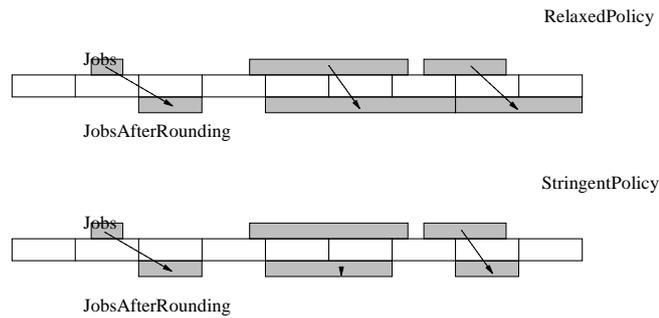


Fig.2. Two rounding policies.

The unshaded rectangles are time slices. The shaded rectangles represent jobs. The top ones show the requested start and end times. The bottom ones show the rounded start and end times. If a job  $i$  is an old one, its rounded start time  $\hat{S}_i$  is replaced by the current time  $t$ . The remaining demand is updated by subtracting from it the total amount of data transferred for job  $i$  on the previous interval,  $((k-1)\tau, k\tau]$ . By definition, the slice set anchored at each  $t=k\tau$ ,  $G_k$ , contains an infinite number of slices. In general, only a finite subset of  $G_k$  is useful to us. Let  $M_k$  be the index of the last slice in which the rounded end time of some jobs falls. That is,  $M_k = I_k(\max_{i \in J_k} \hat{E}_i)$ . Let  $L_k \subset G_k$  be the collection of time slices  $1, 2, \dots, M_k$ . We call the slices in  $L_k$  as the *active time slices*. We will also think of  $L_k$  as an array (instead of a set) of slices when there is no ambiguity. Clearly, the collection  $\{L_k\}^\infty$  inherits the congruent property from  $\{G_k\}^\infty$ . Therefore, it is sufficient to consider  $\{L_k\}^\infty$  for AC and scheduling.

2.2) Admission Control

For each pair of nodes  $s$  and  $d$ , let the collection of allowable paths from  $s$  to  $d$  be denoted by  $P_k(s,d)$ . In general, the set may vary with  $k$ . For each job  $i$ , let the *remaining demand* at time  $t=k\tau$  be denoted by  $R_k(i)$ , which is equal to the total demand  $D_i$  minus the amount of data transferred until time  $t$ . At  $t=k\tau$ , let  $J \subseteq J_k$  be a sub set of the jobs in the systems. Let  $f_i(p,j)$  be the total flow (total data transfer) allocated to job  $i$  on path  $p$ , where  $p \in P_k(s_i,d_i)$ , on time slice  $j$ , where  $j \in L_k$ . As part of the admission control algorithm, the solution to the following feasibility problem is used to determine whether the jobs in  $J$  can all be admitted.

AC(k, j)

$$- \sum_{j=1}^J \sum_{p \in P_k(s_i, d_i)} f_i(p,j) = R_k, \quad \forall i \in J \tag{3}$$

$$- \sum_{i \in J} \sum_{p \in P_k(s_i, d_i)} f_i(p,j) \leq C_e(j) \text{LEN}_k(j), \quad \forall e \in E, \forall j \in L_k \tag{4}$$

$$- f_i(p,j) = 0, \quad j \in L_k(\square) \text{ or } j > I_k(\hat{E}_i), \quad \forall i \in J, \forall p \in P_k(s_i, d_i) \tag{5}$$

$$- f_i(p,j) \leq 0, \quad \forall i \in J, \forall j \in L_k, \forall p \in P_k(s_i, d_i) \tag{6}$$

(3) says that, for every job, the sum of all the flows assigned on all time slices for all paths must be equal to its remaining demand. (4) says that the capacity constraints must be satisfied for all edges on every time slice. Note that the allocated rate on path  $p$  for job  $i$  on slice  $j$  is  $f_i(p, j)/\text{LEN}_k(j)$ , where  $\text{LEN}_k(j)$  is the length of slice  $j$ . The rate is assumed to be constant on the entire slice. Here,  $C_e(j)$  is the remaining link capacity of link  $e$  on slice  $j$ . (5) is the start and end time constraint for every job on every path. The flow must be zero before the rounded start time and after the rounded end time.<sup>4</sup> Recall that we are assuming every job to be a bulk transfer for simplicity. If job  $i$  is of the MBG class and requests a minimum bandwidth  $B_i$  between the start

and end times, then the remaining capacity constraint (3) will be replaced by the following minimum bandwidth guarantee condition.

$$\sum_{p \in CP_k(s_i, d_i)} f_i(p, j) \leq B, \forall j \in L_k. \quad (7)$$

The AC/scheduling algorithms are triggered every  $\tau$  time units with the AC part be for  $e$  the scheduling part. AC examines the newly arrived jobs and determines their admissibility. In doing so, we need to ensure that the earlier commitments to the old jobs are not broken. This can be achieved by adopting one of the following AC procedures.

**2.2.1) Subtract-Resource (SR):**

An updated (remaining) network is obtained by subtracting the bandwidth assigned to old jobs on future time slices, from the link capacity. Then, we determine a sub set of the new jobs that can be accommodated in this remaining network. This method is helpful to perform quick admission tests<sup>5</sup>. However, it runs the risk of rejecting new jobs that can actually be accommodated by reassigning the flows to the old jobs on different paths and time slices.

**2.2.2) Reassign-Resource (RR):**

This method attempts to reassign flows to the old jobs. First, we cancel the existing flow assignment to the old jobs on the future time slices and rest or  $e$  the network to its original capacity. Then, we determine a sub set of the new jobs that can be admitted along with all the old jobs under the original network capacity. This method is expected to have a better acceptance ratio than SR. However, it is computationally more expensive because the flow assignment is computed for all the jobs in the system, both the old and the new.

The actual admission control is as follows. In the SR scheme, the remaining capacity of link  $e$  on slice  $j$ ,  $C_e(j)$ , is computed by subtracting from  $C_e$  (the original link capacity), the total bandwidth allocated on slice  $j$  for all paths crossing  $e$ , during the previous run of the AC/scheduling algorithms ( $att=(k-1)\tau$ ). In the RR scheme, simply let  $C_e(j)=C_e$ , for all  $e$  an  $dj$ . In the SR scheme, we list the *new* jobs,  $J^n$ , in a sequence,  $1, 2, \dots, m$ . The particular order of the sequence is flexible, possibly dependent on some customizable policy. For instance, the order may be arbitrary, or based on the priority the jobs, or based on increasing order of the request times. In a more sophisticated, price-based scheme, the network controller can order the jobs based on the amount of payment per unit of data transferred that a job requester is willing to pay. We apply a binary search to the sequence to find the last job  $j, 1 \leq j \leq m$ , in the sequence such that all jobs before and including it are admissible. That is,  $j$  is the largest index for which the subset of the new jobs  $J = \{ 1, 2, \dots, j \}$  is feasible for  $AC(k, J)$ . All the jobs after  $j$  are rejected. In the RR scheme at time  $t=kt$ , all the jobs are listed in a sequence where the old jobs  $J_k^o$  ahead of the new jobs  $J_k^n$  in the sequence. The order among the old jobs is arbitrary. The order among the new jobs is again flexible. Denote this sequence as  $1, 2, \dots, m$ , in which jobs  $1$  through  $l$  are the old ones. We then apply a binary search to the sequence of *new* jobs,  $l+1, l+2, \dots, m$ , to find the last job  $j, l < j \leq m$ , such that all jobs before and including it are admissible. That is,  $j$  is the largest index for which the resulting subset of the jobs  $J = \{ 1, 2, \dots, l, l+1, \dots, j \}$  is feasible for  $AC(k, J)$  under the original network capacity.

**III. Discussion**

The binary search technique assumes a pre-defined list of jobs and identifies the first  $j$  jobs that can be admitted into the system without violating the deadline constraints. The presence of an exceptionally large job with unsatisfiable demand will cause other jobs following it to be rejected, even though it may be possible to accommodate them after removing the large job. The rejection ratio tends to be higher when the large job lies closer to the head of the list. An interesting problem is how to admit as many new jobs as possible, after all the old jobs are admitted. This combinatorial problem appears to be quite difficult. One can always use a standard integer programming formulation and solution for it. We do not know any solution techniques that run faster than the integer programming techniques. But, a solution to this problem is orthogonal to the main issues addressed in this paper and, once found, can always be incorporated into our general AC/scheduling frame work. We now comment on the computation complexity for the admission control,  $AC(k, J)$ . If standard linear programming techniques are used, such as the Simplex method, the practical computation time depends on the number of variables and the number of constraints. In  $AC(k, J)$ , the number of variables is no more than  $|J| \times M \times P$ . Here,  $P$  is the maximum number of paths allowed for any job.  $M$  is the maximum number of (future) time slices that need to be considered. It depends on how far into the future advance reservations can be allowed, e.g., three months, and on the type of the congruent slice structure used. The value of  $|J|$  depends on whether SR or RR is used. In the former case, it is equal to the number of new job requests that have arrived on an interval of

length  $\tau$ ; in the latter case, it is equal to all the jobs in the system, including both the old jobs and the new requests. The number of non-trivial constraints is no more than  $|J|+|E|\times M$ , where  $|E|$  is the number of edges in the network. To reduce the execution time of the admission control algorithm, we need to limit the number of paths allowed per job, the number of time slices and the number of jobs that need to be considered. In Section 4.3, we show by experimental results that having 4 to 10 paths per job is generally sufficient to achieve near-optimal performance for research networks. If ever needed, SR is a way of reducing the number of jobs that need to be considered. What remains is how to reduce the number of time slices while not sacrificing performance by much. Section 3 is dedicated to that purpose. Section 4 will continue to address the complexity issue in terms of the algorithm execution time obtained experimentally.

### 2.3) Scheduling Algorithm

Given the set of admitted jobs,  $J^a$ , which always includes the old jobs, the scheduling algorithm allocates flows to these jobs to optimize a certain objective. We consider two objectives, **Quick-Finish** (QF) and **Load-Balancing** (LB). Given a set of admissible jobs  $J$ , the problem associated with the former is subject to (3)-(6).

#### Quick-Finish(k,J)

$$\text{Min} \sum_{j \in L_k} \gamma(j) \sum_{i \in J} \sum_{p \in P_k(s_i, d_i)} f_i(p, j) \quad (8)$$

In the above,  $\gamma(j)$  is a weight function increasing in  $j$ , which is chosen to be  $\gamma(j)=j+1$  in our experiments. In this problem, the cost increases as time increases. The intention is to finish a job early rather than later, when it is possible. The solution tend stop ack more flows in the earlier slices but leaves the load light in later slices. The problem associated with the LB objective is,

#### Load-Balancing(k,J)

$$\text{Max } Z \quad (9)$$

Subject to  $M_k$

$$\sum_{j=1}^k \sum_{p \in P_k(s_i, d_i)} f_i(p, j) = Z R_k(i), \forall i \in J \quad (10)$$

(4)-(6).

Let the optimal solution be  $Z^*$  and  $f_i^*(p, j)$  for all  $i, j$  and  $p$ . The actual flows assigned are  $f_i^*(p, j) / Z^*$ . Note that (10) ensures that  $f_i^*(p, j) / Z^*$  satisfies (3). Also,  $Z^* \geq 1$  must be true since  $J$  is admissible. Hence,  $f_i^*(p, j) / Z^*$  are feasible solution to the **AC(k,J)** problem. The Load-Balancing(k, J) problem above is written in the maximizing concurrent throughput form. It reveals its load-balancing nature when written in the equivalent minimizing congestion form. For that, make a substitution of variables,  $f_i(p, j) \leftarrow f_i(p, j) / Z$ , and let  $\mu = 1 / Z$

We have,

#### Load-balancing-1(k, J)

$$\text{Min } \mu \quad (11)$$

$$\text{Subject to } \sum_{i \in J} \sum_{p \in P_k(s_i, d_i)} f_i(p, j) \leq \mu C_e(j) L E N_k(j), \quad \forall e \in E, \forall j \in L_k \quad (12)$$

(3), (5) and (6).

Hence, the solution minimizes the worst link congestion across all time slices in  $L_k$ .

The scheduling algorithm is to apply  $J=J^a$  to **Quick-Finish** (k,J) or **Load-Balancing** (k,J). This determines an optimal flow assignment to all jobs on all allowed paths and on all time slices. Given the flow assignment  $f_i(p, j)$ , the allocated rate on each time slice is denoted by  $x_i(p, j) = f_i(p, j) / L E N_k(j)$  for all  $l_j \in L_k$ . The remaining capacity of each link on each time slice is given by,

$$C_e(j) = C_e - \sum_{i \in J} \sum_{p \in P_k(s_i, d_i)} x_i(p, j) \quad \text{if SR} \\ C_e \quad \text{if RR} \quad (13)$$

Finally, the complexity of the scheduling algorithms can be analyzed similarly as for the admission control algorithm. The general conclusion is also similar.

## 2.4) Putting It Together: The AC and Scheduling Algorithms

In this section, we integrate various algorithmic components and present the complete AC and scheduling algorithms. On the interval  $((k-1)\tau, k\tau]$ , the system keeps track of the new requests arriving on that interval. It also keeps track of the status of the old jobs. If an old job is completed, it is removed from the system. If an old job is serviced on the interval, the amount of data transferred for that job is recorded. At  $t=k\tau$ , the steps described in Algorithm 1 are taken. Finally, in Figure 3, we show a very simple example of the AC and scheduling algorithms at work. The network has only one link with a capacity of 10 Gbps. The US is used and the AC/scheduling interval length is  $\tau=100s$ . QF is used for scheduling. The top figure shows the job requests. The sizes of job 1 and 2 are 3 terabits and 500 gigabits, respectively. The requested start and end times are 100s and 700s for job 1 and 200s and 300s for job 2. In this case, job 1 is admitted at  $t=100s$ . The middle figure shows the schedule at  $t=100s$ . At  $t=200s$ , job 2 is also admitted. The bottom figure shows the schedule at  $t=200s$ . Note that, by  $t=200s$ , 1 terabits of data have already been transferred for job 1. Note also how the bandwidth assignment for job 1 is changed at  $t=200s$ ,

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### Algorithm 1 Admission Control and Scheduling

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- 1: Construct the anchored slice set at  $t=k\tau, G_k$ .
  - 2: Construct the job sets  $J_k$ ,  $J_o$  and  $J_n$ , which are the collection of all jobs, the collection of old jobs, and the collection of new jobs in the system, respectively.
  - 3: For each old job  $i$ , update the remaining demand  $R_k(i)$  by subtracting from it the amount of data transferred for  $i$  on the interval  $((k-1)\tau, k\tau]$ . Round the start time  $s$  as  $\hat{S}_i=t$ .
  - 4: For each new job  $l$ , let  $R_k(l)=D_l$ . Round the requested start and end time according to (1) and (2), depending on whether the stringent or relaxed rounding policy is used. This produces the rounded start and end times,  $\hat{S}_l$  and  $\hat{E}_l$ .
  - 5: Derive  $M_k = I_k (\max_{i \in J_k} \hat{E}_i)$ . This determines the finite collection of slices  $L_k = \{1, 2, \dots, M_k\}$ , the first  $M_k$  Slices of  $G_k$ .
  - 6: Perform admission control as in Algorithm 2. This produces the list of admitted jobs  $J_k^a$ .
  - 7: Schedule the admitted jobs as in Algorithm 3. This yields the flow amount  $f_i(p, j)$  for each admitted job  $i \in J_k^a$ , over all paths for job  $i$ , and all time slices  $j \in L_k$ .
  - 8: Compute the remaining network capacity by (13).
- 

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### Algorithm 2 AC-Step 6 of Algorithm 1

---

- 1: **if** Subtract-Resource is used **then**
  - 2: Sequence the *new* jobs ( $J^n$ ) in the system. Denote the sequence by  $(1, 2, \dots, m)$ .
  - 3: Find the last job  $j$  in the sequences that the set of jobs  $J = \{1, 2, \dots, j\}$  is admissible by  $AC(k, J)$ .
  - 4: **else if** Reassign-Resource is used **then**
  - 5: Apply binary search to the subsequence of new jobs  $(1+1, 1+2, \dots, m)$ . Find the last job  $j$  in the subsequences that the set of jobs  $J = \{1, 2, \dots, j\}$  is admissible by  $AC(k, J)$ .
  - 6: **end if**
  - 7: Return the admissible set,  $J_k^a = J$ .
- 

---

### Algorithm 3 Scheduling-Step 7 of Algorithm 1

---

- 1: **if** Quick-Finish is preferred **then**
  - 2: Solve **Quick-Finish** ( $k, J_k^a$ )
  - 3: **else**
  - 4: Solve **Load-Balancing** ( $k, J_k^a$ )
  - 5: **end if**
-

When compared to that at  $t=100s$ . This is in response to the admission of job 2, which has a stringent end time requirement. Furthermore, it can be seen that the bandwidth assignment for job 1 is time-varying.

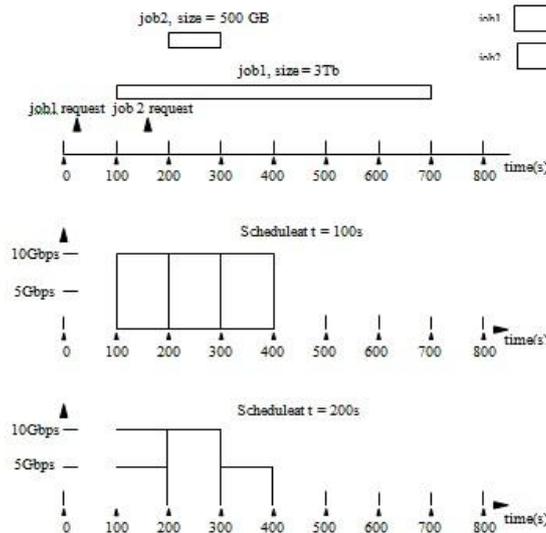


Fig.3. An AC and scheduling example for a network with one link with a capacity 10 Gbps

#### IV. NON-UNIFORM SLICE STRUCTURE

As discussed in Section 2.1.1 and Section 2.2, the number of time slices directly affects the number of variables in our AC and scheduling linear programs, and in turn the execution time of our algorithms. We face a problem of covering a large enough segment of the time line for advance reservations with a small number of slices, say about 100. In this section, we will design a new slice structure with non-uniform slice sizes. They contain a geometrically (exponentially) increasing subsequence, and therefore, are able to cover a large time line with a small number of slices. The key is that, as time progresses, coarse time slices will be further divided into finer slices. The challenge is that the slice structure must remain congruent.

Recall that the congruent property means that, if a slice in an earlier anchored slice set overlaps in time with a later anchored slice set, it either remains as a slice, or is partitioned into smaller slices in the later slice set. The definition is motivated by the need for maintaining consistency in bandwidth assignment across time. As an example, suppose at time  $(k-1)\tau$ , a job is assigned a bandwidth  $x$  on a path on the slice  $j_{k-1}$ . At the next scheduling instance  $t=k\tau$ , suppose the slice  $j_{k-1}$  is partitioned into two slices. Then, we understand that a bandwidth  $x$  has been assigned on both slices. Without the congruent property, it is likely that a slice, say  $j_k$ , in the slice set anchored at  $k\tau$  cuts across several slices in the slice set anchored at  $(k-1)\tau$ . If the bandwidth assignments at  $(k-1)\tau$  are different for these latter slices, the bandwidth assignment for slice  $j_k$  is not well defined just before the AC/scheduling run at time  $k\tau$ .

##### 3.1) Nested Slice Structure

In the nested slice structure, there are  $l$  types of slices, known as level- $i$  slices,  $i=1,2,\dots,l$ . Each level- $i$  slice has a duration  $\Delta_i$ , with the property that  $\Delta_i = \kappa_i \Delta_{i+1}$ , where  $\kappa_i > 1$  is an integer, for  $i=1,\dots,l-1$ . Hence, the slice size increases at least geometrically as  $i$  decreases. For practical applications, a small number of levels suffices. We also require that, for  $i$  such that  $\Delta_{i+1} \leq \tau < \Delta_i$ ,  $\tau$  is an integer multiple of  $\Delta_{i+1}$  and  $\Delta_i$  is an integer multiple of  $\tau$ . This ensures that each scheduling interval contains an integral number of slices and that the sequence of scheduling instances does not skip any level- $j$  slice boundaries, for  $1 \leq j \leq i$ .

The nested slice structure can be defined by construction. At  $t=0$ , the time line is partitioned into level-1 slices. The first  $j_1$  level-1 slices, where  $j_1 \geq 1$ , are each partitioned into level-2 slices. This removes  $j_1$  level-1 slices but adds  $j_1 \kappa_1$  level-2 slices. Next, the first  $j_2$  level-2 slices, where  $j_2 \leq j_1 \kappa_1$ , are each partitioned into level-3 slices. This removes  $j_2$  level-2 slices but adds  $j_2 \kappa_2$  level-3 slices. This process continues until, in the last step, the first  $j_{l-1}$  level- $(l-1)$  slices are partitioned into  $j_{l-1} \kappa_{l-1}$  level- $l$  slices. Then, the first  $j_{l-1}$  level- $(l-1)$  slices are removed and  $j_{l-1} \kappa_{l-1}$  level- $l$  slices are added at the beginning. In the end, the collection of slices at  $t=0$  contains  $\sigma_1 \rightarrow j_{l-1} \kappa_{l-1}$  (  $\rightarrow$  means "defined as") level- $l$  slices,  $\sigma_{l-1} \rightarrow j_{l-2} \kappa_{l-2} \rightarrow j_{l-1}$  level- $(l-1)$  slices, ...,  $\sigma_2 \rightarrow j_1 \kappa_1 \rightarrow j_2$  level-2 slices, and followed by an infinite number of level-1 slices. The sequence of  $j_i$ 's must satisfy  $j_2 \leq j_1 \kappa_1$ ,  $j_3 \leq j_2 \kappa_2$ , ...,  $j_{l-1} \leq j_{l-2} \kappa_{l-2}$ . This collection of slices is denoted by  $G_0$ .

As an example, to cover a maximum of 30-day period, we can take  $\Delta_1=1$ day,  $\Delta_2=1$ hour, and  $\Delta_3=10$  minutes. Hence,  $\kappa_1=24$  and  $\kappa_2=6$ . The first two days are first divided into a total 48 one-hour slices, out of which the first 8 hours are further divided into 48 10-minute slices. The final slice structure has 48 level-3 (10-minute) slices, 40 level-2 (one-hour) slices, and as many level-1(one-day) slices as needed, in this case 28. The total number of slices is 116.

1) **At-Least- $\sigma$** : For  $j$  from 1 down to 2, if the number of slices at level  $j, z_j$ , is less than  $\sigma_j$ , bring in (and remove) then extlevel- $(j-1)$  slice and partition it into  $\kappa_{j-1}$  level- $j$  slices. This scheme maintains atleast  $\sigma_j$  and atmost  $\sigma_j + \kappa_{j-1} - 1$  level- $j$  slices for  $j=2, \dots, l$ .

2) **At-Most- $\sigma$** : In this scheme, we try to bring the current number of slices at level  $j, z_j$ , to  $\sigma_j$ , for  $j=2, \dots, l$ , subject to the constraint that new slices at level  $j$  can only be create d if  $t$  is an integer multiple of  $\Delta_{j-1}$ . More specifically, at  $t=\kappa\tau$ , the following is repeated for  $j$  from 1 down to 2. If  $t$  is *not* an integer multiple of  $\Delta_{j-1}$ , then nothing is done. Otherwise, if  $z_j < \sigma_j$ , we try to create level- $j$  slices out of a level- $(j-1)$  slice. In the creation process, if a level- $(j-1)$  slice exists, then bring in the first one and partition it. Other wise, we try to create more level- $(j-1)$  slices, provided  $t$  is an integer multiple of  $\Delta_{j-2}$ . Hence, are cursive slice-creation process may be involved.

Fig. 4 and 5 show a two-level and three-level nested slice structure, respectively under the At-Most- $\sigma$  design. In the special but typical case of  $\sigma_j > \kappa_{j-1}$ , for  $j=2, \dots, l$ , the At-Most- $\sigma$  algorithm can be simplified as follows. For  $j$  from 1 down to 2, if  $z_j \leq \sigma_j - \kappa_{j-1}$ , bring in (and remove) then extlevel- $(j-1)$  slice and partitionit into  $\kappa_{j-1}$  level- $j$  slices This scheme maintains atleast  $\sigma_j - \kappa_{j-1}$  and atmost  $\sigma_j$  level- $j$  slices for  $j=2, \dots, l$ .

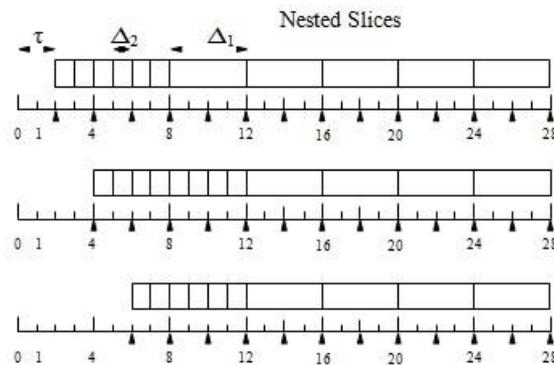


Fig.4. Two-level nested time-slice structure.  $\tau=2, \Delta_1=4$  and  $\Delta_2=1$ .The anchored slice sets shown are for  $t=\tau, 2\tau$  and  $3\tau$ , respectively. At-Most- $\sigma$  Design.  $\sigma_2=8$ .

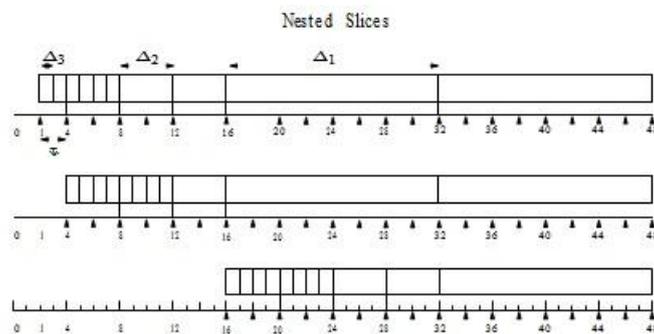


Fig.5. Three-level nested time-slice structure  $\tau=2, \Delta_1=16, \Delta_2=4$  and  $\Delta_3=1$ . The anchored slice sets shown are for  $t=\tau, 2\tau$  and  $8\tau$ , respectively. At-Most- $\sigma$  Design.  $\sigma_3=8, \sigma_2=2$ .

### 3.2) Variant of Nested Slice Structure

When some  $\kappa_j$  is large, it may be unappealing that the number of level- $j$  slices varies by  $\kappa_{j-1}$  (some times more than  $\kappa_{j-1}$ ). To solve this problem, we next introduce another congruence slice structure related to the nested slice structure. We will called it the **Almost- $\sigma$  Variant** of the nested slice structure, because it maintains atleast  $\sigma_j$  and atmost  $\sigma_j + 1$  level- $j$  slices for  $j=2, \dots, l$ .

The Almost- $\sigma$  Variant starts the same way as the nested slice structure at  $t=0$ . As time progresses

from  $(k-1)\tau$  to  $k\tau$ , for  $k=1,2,\dots$ , the collection of slices anchored at  $t=k\tau$ , i.e.,  $G_k$ , is updated from  $G_{k-1}$  as in algorithm 4. The price to pay is that the Almost- $\sigma$  Variant introduces new slice types different from the pre-defined level-I slices, for  $i=1,\dots,l$ . Fig.6 shows a three-level Almost- $\sigma$  Variant.

**Algorithm 4** Almost- $\sigma$ -Variant

- 1: **for**  $j=1$  down to 2 **do**
- 2: **if**  $z_j < \sigma_j$  **then**
- 3: Bring in (and remove) the next available slice of a larger size and create additional  $\sigma_j - z_j$  level- $j$  slices.
- 4:  $z_j \leftarrow \sigma_j$ .
- 5: The remaining portion of the removed level- $(j-1)$  slice forms another slice.
- 6: **endif**
- 7: **endfor**

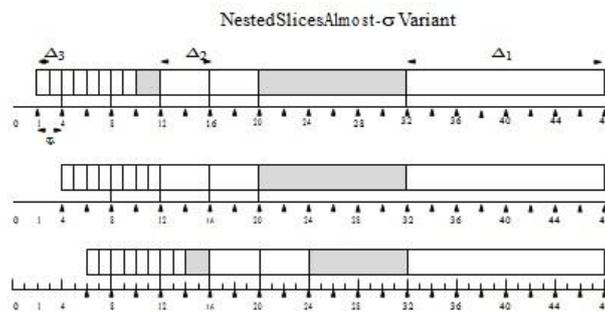


Fig.6. Three-level nested slice structure Almost- $\sigma$  Variant.  $\tau=2$ ,  $\Delta_1=16$ ,  $\Delta_2=4$  and  $\Delta_3=1$ . The anchored slice sets shown are for  $t=\tau$ ,  $2\tau$  and  $3\tau$ , respectively.  $\sigma_3=8$ ,  $\sigma_2=2$ . The shaded are as a real so slices, but are different in size from any level- $j$  slice,  $j=1,2$  or  $3$ .

**V. EVALUATION**

This section describes the performance results of different variations of our AC/scheduling algorithms. We also evaluate the required computation time to determine the scalability of our algorithms. Most of the experiments are conducted on the Abilene network, which consists of 11 back bone nodes connected by 10 Gbps links. Each back bone node is connected to a randomly generated stub network. The link speed between each stub network and the back bone node is 1 Gbps. The entire network has 121 nodes and 490 links. For the scalability study of the algorithms, we use random networks with the number of nodes ranging from 100 to 1000. The random network generator takes the number of nodes and the average node degree as arguments, from which it computes the total number of links in the network. Then, it repeatedly picks a node pair uniformly at random from those unconnected node pairs, and connects them with a pair of links in both directions. This process is repeated until a ll links are assigned. We use the commercial CPLEX package for solving linear programs on Intel-based. The plots and tables use acronyms to denote the algorithms used in the experiments. Recall that SR stands for Subtract-Resource and RR stands for Reassign-Resource in admission control; LB stands for Load-Balancing as the scheduling objective and QF stands for Quick-Finish.

**The performance measures are:**

- Rejection ratio: This is the ratio between the number of jobs rejected and total number of job requests. From the network’s perspective, it is desirable to admit as many jobs as possible.
- Response time: This is the difference between the completion time of a job and the time when it is first being transmitted. From an individual job’s perspective, it is desirable to have shorter response time.

**4.1) Comparison of Algorithm Execution Time**

Before comparing the performance of the algorithms, we first compare their execution time. Short execution time is important for the practicality of our centralized network control strategy. The results on the execution

time put the performance comparison (Section 4.2) in perspective: Better performance often comes with longer execution time. Table I shows the execution time of different schemes under two representative traffic conditions. <sup>6</sup>We ignore the connection setup (path setup) time because, due to the small network size, we can pre-compute and store the allowed paths for every possible source-destination pair.

TABLE I  
AVERAGE AC/SCHEDULING ALGORITHM EXECUTION TIME(S)

Algorithm	HeavyLoad		LightLoad	
	AC	Scheduling	AC	Scheduling
US+SR+LB	13.13	5.70	0.40	0.61
US+SR+QF	12.03	1.86	0.32	0.23
US+RR+LB	80.89	5.89	1.05	0.65
US+RR+QF	34.36	4.74	0.36	0.21
NS+SR+LB	1.54	4.50	0.14	0.60
NS+SR+QF	1.57	1.60	0.13	0.07
NS+RR+LB	25.16	4.30	1.07	0.61
NS+RR+QF	17.43	3.54	0.17	0.06

**4.1.1) SR vs RR and LB vs QF:**

The results show that, for admission control, SR can have much shorter average execution time than RR. This is because, in SR, AC works only on the new jobs, whereas in RR, AC works on all the jobs currently in the system. Hence, for SR the AC (k, J) feasibility problem usually has much fewer variables.

When the AC algorithm is fixed, the choice of the scheduling algorithm, LB or QF, also affects the execution time for AC. For instance, the RR+LB combination has much longer execution time for AC than the RR+QF combination. This is because, in LB, each job tends to be stretched over time in an effort to reduce the network load on each time slice. This results in more jobs and more active slices (slices in  $L_k$ ) in the system at any moment, which means more variables for the linear program. For scheduling, since LB and QF are very different linear programs, it is difficult to explain the differences in their execution time. But, we do observe that LB has longer execution time, again possibly due to more variables for the reason stated in the previous paragraph.

**4.1.2) US vs NS:**

Depending on the number of levels for the NS, the number of slices at each level and the slice sizes, the NS can be configured to achieve different objectives: improving the algorithm performance, reducing the execution time, or doing both simultaneously. Our experimental results in Table I correspond to the third case. Since the two-level NS structure has  $\Delta_1=60$  minutes and the US has the uniform slice size  $\Delta=21.17$  minutes, the NS typically has fewer slices than the US. For instance, under heavy load, US+RR+QF uses 150.5 active slices on average for AC, while NS+RR+QF uses 129.6 active slices on average. The number of variables, which directly affect the computation time of the linear programs, is generally proportional to the number of slices.

Part of the performance advantage of the NS (to be shown in Section 4-2) is attributed to the smaller scheduling interval  $\tau$ . To reduce the scheduling interval for the US, we must reduce the slice size  $\Delta$ , since  $\Delta=\tau$  in the US. In the next experiment, we set the US slice size to be 5 minutes, which is equal to the size of the finer slice in the NS. Table II shows the performance and execution time compare is on between the US and NS. Here, we use RR for admission control and QF for Scheduling. The US and NS have nearly identical performance in terms of the response time and job rejection ratio. But the NS is far superior in execution times for both AC and scheduling. Upon closer inspection (Table III), the NS requires far fewer active time slices than the US on average.

TABLEII  
COMPARISON OF US AND NS ( $\tau=5$  MINUTES)

	Response Time(min)	Rejection Ratio	ExecutionTime(s)	
			AC	Scheduling
LIGHTLOAD				
US	6.064	0	0.469	0.309
NS	5.821	0	0.162	0.062
MEDIUMLOAD				
US	9.767	0.006	3.177	2.694
NS	9.354	0.006	0.587	0.387
HEAVYLOAD				
US	16.486	0.183	131.958	26.453
NS	17.107	0.173	17.428	3.539

TABLEIII  
AVERAGE NUMBER OF SLICES OF US AND NS ( $\tau=5$  MINUTES)

		AverageNumberofSlices	
		AC	Scheduling
LightLoad	US	299.0	299.9
	NS	68.9	69.0
MediumLoad	US	421.6	462.9
	NS	79.1	82.1
HeavyLoad	US	975.1	799.8
	NS	129.6	113.4

In summary,

- SR is much faster than RR for admission control.
- LB tends to be slower than QF for both AC and scheduling.
- The NS requires much shorter execution time than the US, or achieves better performance or has both properties.

The advantage of the NS can be extended by increasing the number of slice levels. In practice, it is likely that the US is too time consuming and the NS is a must.

#### 4.2) Performance Comparison of the Algorithms

In this subsection, the experimental parameters are as stated in the introduction for Section 4. In particular, we fix the number of paths per job (K) to be 8. Table IV shows the response time and rejection ratio of different algorithms.

TABLEIV  
PERFORMANCECOMPARISONOFDIFFERENTALGORITHMS

Algorithm	Light Load		Medium Load		Heavy Load	
	Response Time(s)	Rejection Ratio	Response Time(s)	Rejection Ratio	Response Time(s)	Rejection Ratio
US+SR+LB	46.55	0	42.35	0.056	35.56	0.423
US+SR+QF	21.51	0.014	22.21	0.100	23.56	0.477
US+RR+LB	46.55	0	40.73	0.026	35.73	0.313
US+RR+QF	21.55	0	23.36	0.021	25.16	0.312
NS+SR+LB	49.60	0	43.83	0.021	28.74	0.237
NS+SR+QF	5.73	0.006	7.56	0.052	11.06	0.403
NS+RR+LB	49.60	0	43.88	0.011	30.16	0.168
NS+RR+QF	5.82	0	9.35	0.006	17.11	0.173

#### 4.2.1) US vs NS:

In Table IV, the algorithms with the NS have a comparable to much better performance than those with the US. Furthermore, it has already been established in Section 4- 1 that the NS has much shorter algorithm execution time.

#### 4.2.2) Best Performance:

The best performance in terms of both response time and the rejection ratio is achieved by the RR+QF combination. Suppose we fix the slice structure and the scheduling algorithm. Then, SR has worse rejection ratio than RR because SR does not allow flow reassignment for the old jobs during the admission control. Since response time increases with the admitted traffic load, an algorithm that leads to lower rejection ratio can have higher response time. This explains why RR often has higher response time than the corresponding SR algorithm. Note that a lower rejection ratio does not *always* lead to higher traffic load since some algorithms such as RR use the network capacity more efficiently.

Suppose we fix the slice structure and the AC algorithm. Then, LB does much worse than QF in terms of response time, because LB tends to stretch a job until its requested end time while QF tries to complete a job early if possible. If RR is used for admission control, then under high load, the different scheduling algorithms have a similar effect on the rejection ratio of the next admission control operation. However, for medium load we notice that the work conserving nature of QF contributes to a lower rejection ratio than LB, which tends to waste some bandwidth.

#### 4.2.3) Merits of SR and LB:

Given the above discussion, one may quickly dismiss SR and LB. But, as we have noted in Section 4-1, SR can have considerably shorter execution time than RR. Furthermore, it is a candidate for conducting real time admission control at the instance when a request is made, which is not possible with RR. If SR is used, then LB often has a lower rejection ratio than QF. The reason is that QF tends to highly utilize the network on earlier time slices, making it more likely to reject small jobs requested for the near future. This is a legitimate concern because in practice it is more likely that small jobs are requested to be completed in the near future rather than the more distant future.

There is indication that the more heavy-tailed is the file size distribution, the larger is the difference in rejection ratio between LB and QF. The evidence is shown in Fig.7 for the light traffic load. As the Pareto parameter  $\alpha$  approaches 1 while the average job size is held constant the chance of having very large files increases. Even if they are transmitted at the full network capacity as in QF such large files can still congest the network for a long time causing more future jobs to be rejected. The correct thing to do if SR is used is to spread out the transmission of a large file over its requested time interval.

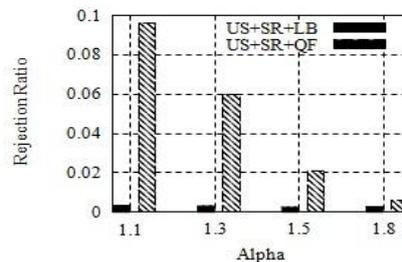


Fig.7 Rejection ratio for different  $\alpha$ 's under SR

To summarize the key points between the admission control methods RR is much more efficient in utilizing the network capacity which leads to fewer jobs being rejected while SR is suitable for fast or real time admission control if SR is used for admission control then the scheduling method LB is superior to QF in terms of the rejection ratio.

#### 4.3) Single vs Multi-path Scheme

The effect of using multiple paths is shown in Fig.8 for the light, medium and heavy traffic loads. Here the NS is used along with the admission control scheme RR and the scheduling objective QF. For every source-destination node pair the K shortest paths between the nodes are selected and used by every job between the node pair. We vary K from 1 to 10 and find that multiple paths often produce better response time and always produce a lower rejection ratio. The amount of improvement depends on many factors such as the traffic load, the version of the algorithm and the network parameters. For the light load no job is rejected. As the number of paths per job increases from 1 to 8 we get 35% reduction in the response time. No further improvement is gained with more than 8 paths. For the medium load the response time is almost halved as the number of paths varies from 1 to 10.

The improvement in the rejection ratio is even more impressive from 13.3% down to 0.3%. For the heavy load there is no improvement in the response time due to the significant reduction in the rejection ratio with multiple paths many more jobs are admitted resulting in a large increase of the actual network load.

Fig.9 and Fig.10 show the response time and the rejection ratio respectively under the medium traffic load for all algorithms. It is observed that the rejection ratio decreases significantly for all algorithms as K increases. All the algorithms that use LB for scheduling experience an increase in the response time due to the reduction in the rejection ratio. But this is not a disappointing result because it is not a goal of LB to reduce the response time. All the algorithms using QF for scheduling experience a decrease in the response time. In spite of the increased load QF is able to pack more jobs in earlier slices by utilizing the additional paths.

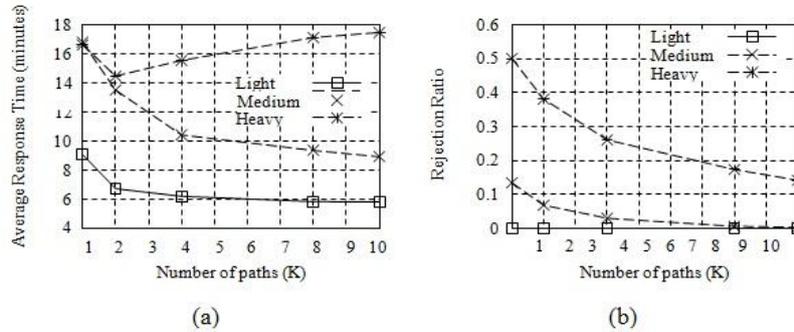


Fig.8 Single vs multiple paths under different traffic load (a) Response time(b)Rejection ratio.

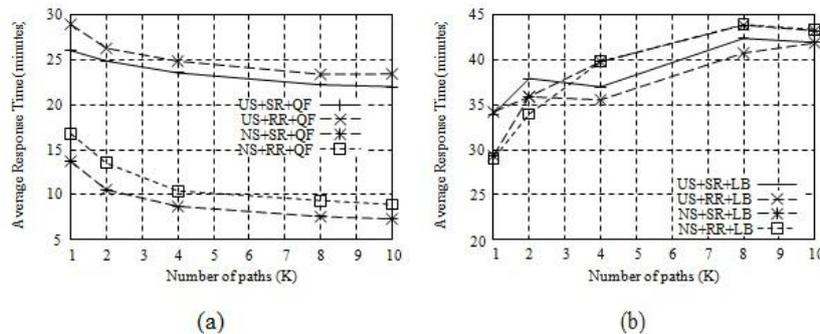


Fig.9 Single vs multiple paths under medium traffic load for different algorithms (a) Response time for QF (b) Response time for LB.

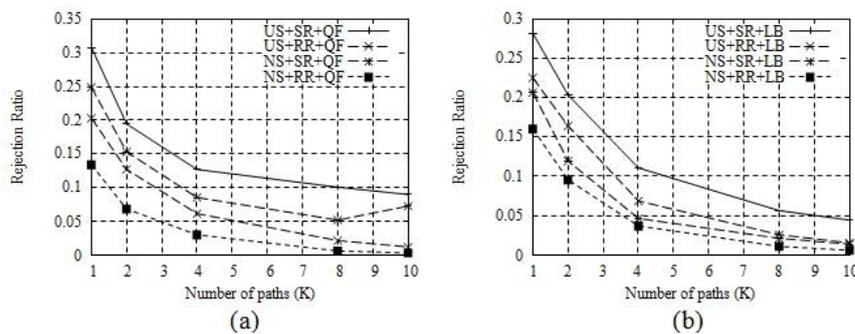


Fig.10 Single vs multiple paths under medium traffic load for different algorithms (a) Rejection ratio for QF (b) Rejection ratio for LB

#### 4.4) Comparison against Typical AC/Scheduling Algorithm

The next experiment compares our AC/scheduling algorithms with a simple incremental AC/scheduling algorithm which will be called the *simple scheme*. The simple scheme couples AC from routing and assumes a single default path given by the routing protocol. AC is conducted in real time upon the arrival of a request. The requested resource is compared with the remaining resource in the network on the default path. If the latter is sufficient then the job is admitted. The remaining resource is updated by subtracting from it what is allocated to the new request by the scheduling step (See next).

Compared to our AC/scheduling algorithms the simple scheme resembles our SR admission control algorithm but allows only one path for each job. For bulk transfer with start and end time constraints the simple scheme still requires a scheduling stage because bandwidth needs to be allocated to the newly admitted job over the time slices on its default path. We can apply the time slice structure and the scheduling objective of LB or

QF to the newly admitted job. However unlike our scheduling algorithm the scheduling algorithm in the simple scheme does not reschedule the *old* jobs that is it does not change the bandwidth allocation for the old jobs.

The reason we use the simple scheme as the base line for comparison with our algorithms is that it is fairly general. The basic part of the simple scheme is really what most other systems or proposals use. If we remove the advance reservation part the AC in the simple scheme resembles a typical AC algorithm proposed for most traditional QoS architectures for large networks [23],[24],[25],[26]. With advance reservation it is similar to most proposals for AC in research networks [13],[22]. But compared with most other schemes the simple scheme has some thing extra. The bandwidth for a job can be different from slice to slice. Hence the performance of the simple scheme is atleast as good as and nearly always better than that of other exiting schemes.

Table V shows the rejection ratio of the simple scheme with different slice structures and scheduling algorithms for different traffic loads. This should be compared with Table IV. The simple scheme leads to considerably higher rejection ratios than all of our algorithms involving SR which in turn have higher rejection ratios than the corresponding algorithms involving RR.

TABLE V  
REJECTION RATIO OF THE SIMPLE SCHEME

	LightLoad	MediumLoad	HeavyLoad
US+SR+LB	0.010	0.345	0.781
US+SR+QF	0.031	0.308	0.792
NS+SR+LB	0	0.225	0.596
NS+SR+QF	0.026	0.249	0.642

#### 4.5) Scalability of AC/Scheduling Algorithms

For this experiment we assume that all job requests arrive at the same time and have the same start and end time requirement. Hence the AC/scheduling algorithms run only once. The objective is to determine how the execution time of the algorithms scales with the number of simultaneous jobs in the system the number of time slices used or the network size. In this case RR and SR are indistinguishable. In the following results we use the US+SR+QF scheme.

Fig.11 shows the execution time of AC and scheduling as a function of the number of jobs. The interval between the start and end times is partitioned into 24 uniform time slices. It is observed that the increase in the execution time is linear or slightly faster than linear. Scaling upto thousands of simultaneous jobs appears to be possible.

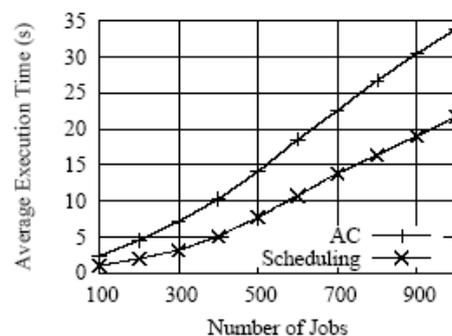


Fig.11 Scalability of the execution times with the number of jobs

## VI. RELATEDWORK

Compared with the traditional QoS frameworks such as InterServ[27], DiffServ[28] the ATM network[23] or MPLS[24] admission control and scheduling for research networks are recent concerns with much fewer published studies.

### 5.1) Bulk Transfer

Recent papers on AC and scheduling algorithms for bulk transfer with advance reservations include [14],[15], [16],[17],[18],[19],[13],[20],[21]. In [13] the AC and scheduling problem is considered only for the single link case. Network-level AC and scheduling are considered to be outside the scope of [13]. As a result multi-path routing and network-level bandwidth allocation and re-allocation have no counter-part in [13]. Moreover the solution is a heuristic one instead of an optimal one. Finally once a job is admitted permanently it

won't be reconsidered in the future. In contrast we periodically re-optimize the bandwidth assignment for all the new and old jobs.

The authors of [21] propose a malleable reservation scheme for bulk transfer which checks every possible interval between the requested start time and end time for the job and tries to find a path that can accommodate the entire job on that interval. The scheme favors intervals with earlier dead lines. In [20], the computational complexity of a related path-finding problem is studied and an approximation algorithm is suggested. [15] starts with an advance reservation problem for bulk transfer. Then the problem is converted into a constant bandwidth allocation problem at a single time instance to maximize the job acceptance rate. This is shown to be an NP-hard problem. Heuristic algorithms are then proposed. In [15], all the requests are known at the time of the admission control and no that the requests continue to arrive and the AC/scheduling must be done repeatedly. The concern for us is how to optimize and re-optimize the bandwidth assignment to the jobs as new job requests arrive, so that the early commitments are not violated and the network resource is used efficiently. In [15], the bandwidth constraints are at the ingress and egress links only. As a result, there is no routing issue. In our case, we have a full network and we use multiple paths for each job. We may alter the bandwidth assignment on the paths for each existing job in the system in order to accommodate later jobs.

### **5.2) MBG Traffic**

Several earlier studies [29],[30],[31],[32] have considered admission control at an individual link for the MBG (minimum bandwidth guarantee) traffic class with start and end times. The concern is typically about designing efficient data structures, such as the segment tree [30], for keeping track of and querying bandwidth usage at the link on different time intervals. The admission of a new job is based on the availability of the requested bandwidth between the job's start time and end time. [20],[33],[21],[34] and [31] go beyond single-link advance reservation and tackle the more general path-finding problem for the MBG class, but typically only for new requests, one at a time. The routes and bandwidth of existing jobs are unchanged. [35] considers a network with known routing in which each admitted job derives a profit. It gives approximation algorithms for admitting a subset of the jobs so as to maximize the total profit.

### **5.3) Other Related Work**

The authors of [36] also advocate periodic re-optimization to determine new bandwidth allocation in optical networks. However, they do not assume that users make advance reservations with requested end times. As a result,[36] does not have the admission control step. In the scheduling step it uses a multi-commodity flow formulation for bandwidth assignment, similar to our formulation but without the time dimension. That is the scheduling problem in [36] is for a single (large) time slice rather than over multiple time slices. Many papers study advance reservation, re-routing, or re-optimization of light paths, at the granularity of a wave length, in WDM optical networks [37],[38]. But they do not consider the start and end time constraint.

### **5.4) Control Plane Protocols, Architectures and Tools**

This paper focuses on the AC and scheduling *algorithms*. A complete solution for the intended e-science application will also need the control plane protocols, architectures and middleware tool kits, which are considered outside the scope of the paper. In the control plane, [22] presents an architecture for advance reservation of intra and inter domain light paths. The DRAGON project [11] develops control plane protocols for multi-domain traffic engineering and resource allocation on GMPLS-capable [39] optical networks. GARA [9], the reservation and allocation architecture for the grid computing tool kit Globus [10], supports advance reservation of network and computing resources. [40] adapts GARA to support advance reservation of light paths, MPLS paths and DiffServ paths. Grid JIT [41] is another signaling protocol for setting up and managing light paths in optical networks for grid-computing applications. ODIN [42] is a tool kit for optical network control and management for supporting grid computing. Another such tool kit is reported in [43]. [44] discusses the architectural and signaling-protocol issues for advance reservation of network resources.

## **VII. CONCLUSION**

This study aims at contributing to the management and resource allocation of research networks for data-intensive e-science collaborations. The need for large file transfer and high-bandwidth, low-latency network paths is among the main requirements posed by such applications. The opportunities lie in the fact that research networks are generally much smaller in size than the public Internet, and hence afford a centralized resource management platform. This paper combines the following novel elements into a cohesive frame work of admission control and flow scheduling advance reservation for bulk transfer and minimum bandwidth guaranteed traffic ,multi-path routing, and bandwidth reassignment via periodic re-optimization.

To handle the start and end time requirement of advance reservation, as well as the advancement of time, we identify a suitable family of discrete time-slice structures, namely, the congruent slice structures. With

such a structure, we avoid the combinatorial nature of the problem and are able to formulate ever all in ear programs as the core of our AC and scheduling algorithms. Moreover, we can develop simple algorithms that can retain the performance guarantee for the existing jobs in the system while admitting new jobs. Our main algorithms apply to all congruent slice structures, which are fairly rich. In particular, we describe the design of the nested slice structure and its variants. They allow the coverage of a long segment of time for advance reservation with a small number of slices without compromising performance. They lead to reduced execution time of the AC/scheduling algorithms, there by making it practical. The following inferences were drawn from our experiments.

- The algorithms can handle upto several hundred time slices with in the time limit imposed by practicality concern. If the NS is used, this number can cover months, even years, of advance reservation with sufficient time slice resolution. If the US is used, either the duration of coverage must be significantly shortened or the time slice be kept very coarse. Either approach tends to degrade the algorithms utility or performance.
- We have argued that between the admission control methods, RR is much more efficient than SR in utilizing the network capacity, thereby, leading to fewer jobs being rejected. On the other hand, SR is suitable for fast or real time admission control. If SR is used for admission control, then the scheduling method LB is superior to QF in terms of the rejection ratio. We have also observed that using multiple paths improves the network utilization dramatically.
- The execution time of our AC/scheduling algorithms exhibits acceptable scaling behavior, i.e., linear or slightly faster than linear scaling, with respect to the network size, the number of simultaneous jobs, and the number of slices. We have high confidence that they can be practical. The execution time can be further shortened by using fast approximation algorithms, more powerful computers and better decomposition of the algorithms for parallel implementation.

Even in the limited application context of e-science, admission control and scheduling are large and complex problems. In this paper, we have limited our attention to a set of issues that we think are unique and important. This work can be extended in many directions. To name just a few, one can develop and evaluate faster approximation algorithms as in [45],[46]; address additional policy constraints for the network usage incorporate the discrete light path scheduling problem develop a price-based bidding system for making admission request or address more carefully the needs of the MBG traffic class, such as minimizing the end-to-end delay.

The AC/scheduling algorithms presented in this paper are only part of a complete solution for the intendede- science applications. Control plane protocols and middleware are needed for settingup the network paths, controlling the bandwidth allocation, and for the end systems to take advantage of the new networking capabilities. The software tools should also automate the user-network interaction, such as the request submission and re-negotiation process. There are several projects in protocol, architecture and toolkit development, mainly in the grid computing community, as discussed in Section 5. Developing similar protocols and adding new components to the existing toolkits in support of our algorithms are among the future tasks.

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